

GUJARAT UNIVERSITY  
B.E. SEM – 3 (EC/IC/BM/CHEM/RUB/PLA/EEE)  
Question Bank  
Applied Maths – II

Each question is of equal Marks (10 Marks)

<b>Q.1</b>	Find the Fourier Series for $f(x) = e^{-x}$ in the interval $0 < x < 2\pi$ .
<b>Q.2</b>	Expand $f(x) = x \sin x$ as a Fourier series in the interval $0 < x < 2\pi$ .
<b>Q.3</b>	Find the Fourier series of $f(x) = 2x - x^2$ in the interval $(0,3)$ . Hence deduce that $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \dots = \frac{\pi^2}{12}$ .
<b>Q.4</b>	Find the Fourier series of the function $f(x) = \begin{cases} x^2 & 0 \leq x \leq \pi \\ -x^2 & -\pi \leq x \leq 0 \end{cases}$ .
<b>Q.5</b>	Find the Fourier series of the function $f(x) = \begin{cases} \pi x & 0 < x < 1 \\ 0 & x = 1 \\ \pi(x-2) & 1 < x < 2 \end{cases}$ . Hence show that $\frac{1}{1} - \frac{1}{3} + \frac{1}{5} - \frac{1}{7} + \dots = \frac{\pi}{4}$ .
<b>Q.6</b>	Find the Fourier series of $f(x) = x^2$ in the interval $0 < x < a$ , $f(x+a) = f(x)$ .
<b>Q.7</b>	If $f(x) =  \cos x $ , expand $f(x)$ as a Fourier series in the interval $(-\pi, \pi)$ , $f(x+2\pi) = f(x)$ .
<b>Q.8</b>	For the function $f(x)$ defined by $f(x) =  x $ , in the interval $(-\pi, \pi)$ . Obtain the Fourier series. Deduce that $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots = \frac{\pi^2}{8}$ .
<b>Q.9</b>	Given $f(x) = \begin{cases} -x+1 & -\pi \leq x \leq 0 \\ x+1 & 0 \leq x \leq \pi \end{cases}$ . Is the function even or odd? Find the Fourier series for $f(x)$ and deduce the value of $\frac{1}{1^2} + \frac{1}{3^2} + \frac{1}{5^2} + \dots$ .
<b>Q.10</b>	Find the Fourier series of the periodic function $f(x)$ ; $f(x) = -k$ when $-\pi < x < 0$ and $f(x) = k$ when $0 < x < \pi$ , and $f(x+2\pi) = f(x)$ .
<b>Q.11</b>	Half range sine and cosine series of $f(x) = x(\pi - x)$ in $(0, \pi)$
<b>Q.12</b>	Find the Fourier series for the function $f(x) = \begin{cases} \pi x, 0 < x < 1 \\ \pi(x-2), 1 < x < 2 \end{cases}$
<b>Q.13</b>	Find the Fourier series for $f(x)$ defined by $f(x) = x + \frac{x^2}{4}$ when $-\pi < x < \pi$ and $f(x+2\pi) = f(x)$ and hence show that $\frac{1}{1^2} - \frac{1}{2^2} + \frac{1}{3^2} - \frac{1}{4^2} + \dots = \frac{\pi^2}{12}$
<b>Q.14</b>	Find the Fourier series for the function $f(x) = \begin{cases} x; 0 < x < 1 \\ 0; 1 < x < 2 \end{cases}$ .

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<b>Q.15</b>	<p>If <math>f(x) = x</math> in <math>0 &lt; x &lt; \frac{\pi}{2}</math></p> <p style="padding-left: 40px;"><math>= \pi - x</math> in <math>\frac{\pi}{2} &lt; x &lt; \frac{3\pi}{2}</math></p> <p style="padding-left: 40px;"><math>= x - 2\pi</math> in <math>\frac{3\pi}{2} &lt; x &lt; 2\pi</math></p> <p>Prove that <math>f(x) = \frac{4}{\pi} \left\{ \frac{\sin x}{1^2} - \frac{\sin 3x}{3^2} + \frac{\sin 5x}{5^2} - \dots \right\}</math></p>
<b>Q.16</b>	<p>If <math>f(x) = \frac{x}{l}</math> when <math>0 &lt; x &lt; l</math></p> <p style="padding-left: 40px;"><math>= \frac{2l-x}{l}</math> when <math>l &lt; x &lt; 2l</math></p> <p>Prove that <math>f(x) = \frac{1}{2} - \frac{4}{\pi^2} \left( \frac{1}{1^2} \cos \frac{\pi x}{l} + \frac{1}{3^2} \cos \frac{3\pi x}{l} + \frac{1}{5^2} \cos \frac{5\pi x}{l} + \dots \right)</math></p>
<b>Q.17</b>	<p>When <math>x</math> lies between <math>\pm\pi</math> and <math>p</math> is not an integer, prove that</p> $\sin px = \frac{2}{\pi} \sin p\pi \left( \frac{\sin x}{1^2 - p^2} - \frac{2 \sin 2x}{2^2 - p^2} + \frac{3 \sin 3x}{3^2 - p^2} - \dots \right)$
<b>Q.18</b>	Find the Fourier series for the function $f(x) = e^{ax}$ in $(-l, l)$
<b>Q.19</b>	Half range sine and cosine series of $f(x) = 2x - 1$ in $(0, 1)$
<b>Q.20</b>	Half range sine and cosine series of $x^2$ in $(0, \pi)$
<b>Q.21</b>	Find Half range sine and cosine series for $f(x) = (x-1)^2$ in $(0, 1)$
<b>Q.22</b>	Evaluate: $L\{\sin 2t \cos 3t\}$ , $L\{e^{-3t}(\cos 4t + \sin 2t)\}$
<b>Q.23</b>	Evaluate: $L\{\sin^2 2t\}$ , $L\{e^{-2t} \cos 3t\}$
<b>Q.24</b>	Evaluate: $L\left\{\frac{\sin 2t - \sin 3t}{t}\right\}$ , $L\left\{t \int_0^t e^{-4t} \sin 3tdt\right\}$

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<b>Q.25</b>	Evaluate: $L^{-1} \left\{ \log \left( \frac{s+1}{s-1} \right) \right\}, L^{-1} \left\{ \frac{s^2 + s + 2}{s^5} \right\}$
<b>Q.26</b>	Evaluate: $L^{-1} \left\{ \cot^{-1} \frac{s}{a} \right\}, L^{-1} \left\{ \frac{s-1}{(s-1)^2 + 4} \right\}$
<b>Q.27</b>	Evaluate: $L^{-1} \left\{ \log \left( \frac{s+2}{s+3} \right) \right\}, L^{-1} \left\{ \frac{s+2}{(s^2 + 4s + 5)^2} \right\}$
<b>Q.28</b>	Evaluate: $L^{-1} \left\{ \frac{1+2s}{(s+2)^2 (s-1)^2} \right\}, L^{-1} \left\{ \frac{s^2 + s + 3}{s^6} \right\}$
<b>Q.29</b>	Evaluate: $L^{-1} \left\{ \frac{(s+1)^2}{s^3} \right\}, L^{-1} \left\{ \tan^{-1} \frac{s}{a} \right\}$
<b>Q.30</b>	Find the Laplace Transform of $f(t)$ , where $(i) f(t) = t \quad \text{if } 0 < t < \frac{a}{2}, \quad f(t+a) = f(t)$ $= a - t \quad \text{if } \frac{a}{2} < t < a$
<b>Q.31</b>	Find the Laplace transform of the function $f(t) = \begin{cases} \sin \omega t; 0 < t < \frac{\pi}{\omega} \\ 0; \frac{\pi}{\omega} < t < \frac{2\pi}{\omega} \end{cases}, \quad f(t) = f\left(t + \frac{2\pi}{\omega}\right)$
<b>Q.32</b>	Use convolution theorem to find the Laplace Inverse Transform of $(i) \frac{sa}{(s^2 - a^2)^2} \quad (ii) \frac{s-2}{s(s-4s-13)}$
<b>Q.33</b>	Use convolution theorem to find the Laplace Inverse Transform of $(i) \frac{s^2}{(s^2 + a^2)(s^2 - b^2)} \quad (ii) \frac{1}{s^2(s-2)}$
<b>Q.34</b>	Find the value of the integral using Laplace Transform technique.

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	(i) $\int_0^{\infty} t e^{-2t} \cos t dt$ (ii) $\int_0^t e^{-t} \frac{\sin t}{t} dt$
<b>Q.35</b>	Solve the initial value problem $y'' + 5y' + 2y = e^{-2t}$ , $y(0) = 1$ , $y'(0) = 1$ , Using Laplace transformation.
<b>Q.36</b>	Solve the following Differential Equations using Laplace Transform technique. $\frac{d^2x}{dt^2} - 2 \frac{dx}{dt} + x = e^t$ with $x = 2$ and $\frac{dx}{dt} = -1$ at $t = 0$
<b>Q.37</b>	Solve the following Differential Equations using Laplace Transform technique. $\frac{d^2y}{dx^2} + y = 1$ with $y(0) = 1$ and $y\left[\frac{\pi}{2}\right] = 0$
<b>Q.38</b>	Solve the following equations : ( a ) $(D - 2)^2 y = 8(e^{2x} + \sin 2x + x^2)$ ( b ) $(D^2 + D) y = x^2 + 2x + 4$
<b>Q.39</b>	Solve the following equations : ( a ) $(D^2 + 1) y = x^2 \cos x$ ( b ) $(D^2 + 1) y = e^{2x} + \cosh 2x + x^3$
<b>Q.40</b>	Solve the following equations : ( a ) $(D^4 + 2D^2 + 1) y = x^2 \cos^2 x$ ( b ) $(D^2 + 2) y = e^{-2x} + \cos 3x + x^2$
<b>Q.41</b>	Solve the following equations : ( a ) $(D^2 + 2D + 1) y = x e^x \sin x$ ( b ) $(D^2 - 9) y = e^{3x} \cos 2x$
<b>Q.42</b>	Solve the following equations : ( a ) $(D - 2)^2 y = 8(e^{2x} + \sin 2x + x^2)$ ( b ) $(D^3 + 8) y = x^4 + 2x + 1$
<b>Q.43</b>	Solve the following equations : ( a ) $(D^2 - 1) y = x \sin 3x + \cos x$ ( b ) $(D^2 - 4D + 4) y = 2e^x + \cos 2x + x^3$
<b>Q.44</b>	Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$ .
<b>Q.45</b>	Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + y = ((\log x) \sin(\log x) + 1) / x$
<b>Q.46</b>	Solve: $(3x + 2) \frac{d^2 y}{dx^2} + 3(3x + 2) \frac{dy}{dx} - 36y = 3x^2 + 4x + 1$ .

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<b>Q.47</b>	Solve: $x^2 \frac{d^2 y}{dx^2} - 3x \frac{dy}{dx} + 5y = x^2 \sin(\log x)$ .
<b>Q.48</b>	Solve: $x^2 \frac{d^2 y}{dx^2} - 2x \frac{dy}{dx} - 4y = x^2 + 2 \log x$ .
<b>Q.49</b>	Solve by using method of variation of parameters: $\frac{d^2 y}{dx^2} + y = \sec x$ .
<b>Q.50</b>	Solve by using method of variation of parameters: $\frac{d^2 y}{dx^2} + y = \tan x$ .
<b>Q.51</b>	Solve by using method of variation of parameters: $\frac{d^2 y}{dx^2} - 2 \frac{dy}{dx} = e^x \sin x$
<b>Q.52</b>	The charge q on a plate of a condenser C is given by $L \frac{d^2 q}{dt^2} + R \frac{dq}{dt} + \frac{q}{c} = E \sin pt$ the circuit is tuned to resonance so that $p^2 = \frac{1}{LC}$ if initially the current i and charge q be zero show that for small value of $\frac{R}{L}$ , the current in the circuit at time t is given by $\left(\frac{Et}{2L}\right) \sin pt$ .
<b>Q.53</b>	Solve the following simultaneous equations: $\begin{matrix} Dx + y = \sin t \\ Dy + x = \cos t \end{matrix}$ ; where $D = \frac{d}{dt}$  given that when $t = 0$ , $x = 1$ and $y = 0$ .
<b>Q.54</b>	Solve the following simultaneous equations: $\begin{matrix} Dx + y = e^t \\ Dy + x = e^{-t} \end{matrix}$ ; where $D = \frac{d}{dt}$
<b>Q.55</b>	Form the partial differential equation of following:  (a) $2z = \frac{x^2}{a^2} + \frac{y^2}{b^2}$ (b) $z = f(x+ct) + g(x-ct)$
<b>Q.56</b>	Form the partial differential equation of following:  (a) $2z = a^2 x^2 + b^2 y^2$ (b) $z = x + y + f(xy)$

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<b>Q.57</b>	Form the partial differential equation of following: (a) $z = (x^2 + a)(y^2 + b)$ (b) $F(xy + z^2, x + y + z) = 0$
<b>Q.58</b>	Solve following partial differential equations : (a) $x(y^2 - z^2)p + y(z^2 - x^2)q = z(x^2 - y^2)$ (b) $x(y - z)p + y(z - x)q = z(x - y)$
<b>Q.59</b>	Solve following partial differential equations : (a) $py + qx = pq$ (b) $z = px + qy + 2\sqrt{pq}$
<b>Q.60</b>	Solve following partial differential equations : (a) $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial x \partial y} = \sin x \cos y + xy$ (b) $\frac{\partial^2 z}{\partial x^2} - \frac{\partial^2 z}{\partial x \partial y} = \cos x \cos 2y$
<b>Q.61</b>	Solve following partial differential equations : (a) $\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = e^{x+4y}$ (b) $\frac{\partial^2 z}{\partial x^2} - 2 \frac{\partial^2 z}{\partial x \partial y} + \frac{\partial^2 z}{\partial y^2} = x^3 + e^{x+2y}$
<b>Q.62</b>	(a) Solve: $\frac{\partial^2 z}{\partial x \partial y} = e^{-y} \cos x$ , given that $z = 0$ when $y = 0$ and $\frac{\partial z}{\partial y} = 0$ when $x = 0$ (b) Solve: $\frac{\partial^2 z}{\partial x^2} = z$ given that $z = e^y$ and $\frac{\partial z}{\partial x} = e^{-y}$ when $x = 0$
<b>Q.63</b>	Solve: $\frac{\partial z}{\partial x} = 2 \frac{\partial z}{\partial y} + z$ where $z(x, 0) = 8e^{-5x}$ using method of separation of variables.
<b>Q.64</b>	Solve: $3 \frac{\partial z}{\partial x} + 2 \frac{\partial z}{\partial y} = 0$ , where $z(x, 0) = 4e^{-x}$ by using method of separation of variables.
<b>Q.65</b>	Solve: $\frac{\partial z}{\partial x} = 4 \frac{\partial z}{\partial y}$ where $z(0, y) = 8e^{-3y}$ using method of separation of variables.
<b>Q.66</b>	(a) Find real root of the equation $x^3 + x^2 + 1 = 0$ by using method of direct iteration correct up to three decimal places. (b) By using Newton –Raphson’s get the real root of the equation $xe^x - 2 = 0$ correct up to two decimal places

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<b>Q.67</b>	<p>(a) Find the real root of the equation <math>x \log_{10} x - 1.2 = 0</math> by false position method.</p> <p>(b) By using Newton –Raphson’s get the real root of the equation <math>x = e^{-x}</math> near <math>x = 0.5</math> correct up to two decimal places.</p>
<b>Q.68</b>	<p>(a) Using the method of iteration, find the roots of the equation <math>x^4 - 3x + 1 = 0</math> <math>x_0 = 1.5</math> correct to four decimal places.</p> <p>(b) Find a root of the equation <math>x^3 - x - 1 = 0</math> correct to three decimal places, using the bisection method.</p>
<b>Q.69</b>	<p>(a) Find root of the equation <math>xe^x = \cos x</math> correct to three decimal places using method of False-position.</p> <p>(b) Find root of the equation <math>x^3 - 3x + 5 = 0</math> correct to three decimal places using method of Newton-Raphson.</p>
<b>Q.70</b>	<p>Find the series solution of the differential equation <math>x \frac{d^2 y}{dx^2} + \frac{dy}{dx} + xy = 0</math></p>
<b>Q.71</b>	<p>Attempt following.</p> <p>1) Express <math>f(x) = 4x^3 + 6x^2 + 7x + 2</math> in terms of Legendre polynomial.</p> <p>2) Prove that <math>J_{\frac{-1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \cos x</math></p>
<b>Q.72</b>	<p>Solve the following equation in power series <math>(1+x^2) \frac{d^2 y}{dx^2} + x \frac{dy}{dx} - y = 0</math></p>
<b>Q.73</b>	<p>Attempt the following.</p> <p>(ii) Evaluate <math>J_{\frac{3}{2}}(x)</math>      (iii) Prove that <math>J_{\frac{-1}{2}}(x) = \sqrt{\frac{2}{\pi x}} \cos x</math></p>
<b>Q.74</b>	<p>Attempt the following.</p> <p>(i) State Rodrigue’s formula for Legendre’s polynomials. Show that <math>P_4(x) = \frac{1}{8}(35x^4 - 30x^2 + 3)</math></p> <p>(ii) Express <math>J_4</math> in terms of <math>J_0</math> and <math>J_1</math>.</p>
<b>Q.75</b>	<p>Solve in series in differential equation <math>\frac{d^2 y}{dx^2} + xy = 0</math></p>
<b>Q.76</b>	<p>Solve in series in differential equation <math>x \frac{d^2 y}{dx^2} + \frac{dy}{dx} - y = 0</math></p>